

## Characterising the within-field scale spatial variation of nitrogen in a grassland soil to inform the efficient design of in-situ nitrogen sensor networks for precision agriculture

Shaw, R.; Lark, R. M.; Williams, A. P.; Chadwick, D. R.; Jones, David

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1    **Characterising the within-field scale spatial variation of different N forms in a**  
2    **grassland soil and the implications for in-situ N sensor technology and precision**  
3    **agriculture**

4

5    R. Shaw<sup>a\*</sup>, R.M. Lark<sup>b</sup>, A.P. Williams<sup>a</sup>, D.R. Chadwick and D.L. Jones<sup>a</sup>

6    <sup>a</sup>*School of Environment, Natural Resources & Geography, Bangor University, Gwynedd,*

7    *LL57 2UW, UK*

8    <sup>b</sup>*British Geological Survey, Keyworth, Nottingham, NG12 5GG*

9

10    *\*Corresponding author*

11    *E-mail address: rory.shaw@bangor.ac.uk: Tel: +44 1248 382579*

## ABSTRACT

The use of in-situ sensors capable of real-time monitoring of soil nitrogen (N) may facilitate improvements in agricultural N-use efficiency (NUE) through better fertiliser management. Optimising the deployment of in-situ sensors for both accuracy and cost requires consideration of the spatial variation of N forms at within-field scales. In this study, a geo-statistical nested sampling approach was used to characterise the spatial variability of amino acids, ammonium ( $\text{NH}_4^+$ ) and nitrate ( $\text{NO}_3^-$ ) in the soil of a grazed grassland field (1.9 ha). Within the growing season, two nested sampling campaigns were undertaken both before and after the application of fertiliser N and the removal of grazing sheep. The field was stratified into four quarters with four mainstations located at random within each quarter. Within each mainstation, sampling at the following spatial scales: 1 cm, 10 cm, 50 cm and 2 m, was performed using a soil corer with a 1 cm diameter. Further investigation into small-scale spatial variance was investigated using smaller soil samples (approx. 70 mg) that represented the “aggregate” scale. Short-range variation was found to be dominant, with at least 61%, 86% and 61% of the total accumulated variance of amino acid-N,  $\text{NH}_4\text{-N}$  and  $\text{NO}_3\text{-N}$ , respectively, occurring at scales  $< 2$  m. Variation at larger scales ( $> 2$  m) was not as significant but was still considered an important spatial component for all N forms. Fertiliser N application and removal of sheep had a small effect on the spatial variance of N forms. In the case of  $\text{NO}_3\text{-N}$ , the total accumulated variance was lower, with more of the observed variance attributed to scales  $> 2$  m. The aggregate-scale sampling revealed further large variation at the sub 1-cm scale. Calculations based on the sampling showed that the  $\text{NO}_3\text{-N}$  field mean could be estimated with a 95% confidence interval of  $1.69 \mu\text{g N g}^{-1}$  using 2 randomly positioned data loggers each with 5 sensors. These calculations assume that the sensor used would sense a similar volume of soil to that sampled by the 1 cm soil corer. Sensors with sensing elements  $< 1$  cm will be subject to further spatial variability and local

37 replication at scales < 1 cm would be needed to maintain accuracy. Therefore, achieving  
38 accurate estimates of the field mean is likely to incur significant costs. Whilst the cost of  
39 technology is likely to decrease, investigation of how best to integrate this approach within a  
40 precision agriculture framework to improve NUE is still required.

41

42 *Keywords:* Dissolved organic nitrogen; Fertilizer management; Nutrient cycling; Soil

43 heterogeneity

**Commented [DLJ1]:** American spelling deliberate here

**Commented [DLJ2]:** Keywords always different from those in the abstract to get more search engine hits.

## 1. Introduction

Improving nitrogen (N) use efficiency (NUE) remains one of the key challenges for global agriculture (Cassman et al., 2002; Robertson and Vitousek, 2009) and is essential for the success of sustainable intensification (Tilman et al., 2011). The deleterious environmental effects and economic costs of diffuse N pollution from farmland in Europe, where N has been applied in excess of crop requirement, are well documented (Sutton et al., 2011).

One often cited approach to reduce N losses and improve NUE, is to ensure synchronicity of N supply with crop demand (Shanahan et al., 2008; Robertson and Vitousek, 2009), although, achieving this in practice is challenging due to the complex nature of the soil-plant system. Precision agriculture (PA) attempts to address this issue by reducing uncertainties surrounding the measurement of key variables to determine optimum N fertiliser management (Pierce and Nowak, 1999; Dobermann et al., 2004). Key to the success of PA is the accurate assessment of within-field soil N status at a high spatial and temporal resolution to enable the variable rate application of N fertiliser. This approach allows areas of N deficiency and surplus to be addressed as well as in-season adjustment of fertiliser rates in accordance with current and predicted growing conditions. However, conventional soil sampling techniques, coupled with laboratory analysis are expensive, labour-intensive, and time-consuming and cannot provide real-time data of sufficient resolution to accurately inform PA management (Sylvester-Bradley et al., 1999; Kim et al., 2009).

A number of different approaches have been used to address this issue. Crop canopy sensing techniques, for determination of plant N status, are now in commercial use and can be used to inform variable rate fertiliser application (e.g. wheat, maize; Raun and Johnson, 1999; Diacono et al., 2013). Whilst the advantages of this approach in some situations have been evidenced (Diacono et al., 2013), plant N status and yield is the product of many variables and may not always correlate with soil mineral N status. On-the-go soil sampling

69 for nitrate, using electrochemical sensor platforms attached to agricultural vehicles have been  
70 developed (Adsett et al., 1999) and, for the case of pH, commercialised (Adamchuk et al.,  
71 1999). The results have been used to develop field nitrate maps (Sibley et al., 2009) which  
72 could be used to define within-field management zones and to calculate variable fertiliser  
73 application rates. On-the-go sampling is generally more spatially intensive than manual field  
74 sampling, allowing better spatial resolution, although key information on how soil mineral N  
75 varies over small spatial scales may not be obtained. This can lead to increased uncertainties  
76 of interpolative predictions, especially if the sample volume is small (Schirrmann and  
77 Domsch, 2011). Furthermore, increasing the temporal resolution of this approach requires  
78 additional economic costs and as both these approaches rely on reactive management, crucial  
79 changes in soil mineral N status may be missed.

80         One approach, which has yet to be explored, is the use of in-situ sensors capable of  
81 monitoring soil mineral N in real time. This approach may enable a step away from  
82 predetermined fertiliser N recommendations (Defra, 2010) to a more dynamic system that  
83 responds in real-time to changes in growing conditions. It potentially has many benefits  
84 compared to on-the-go soil sampling and crop canopy sensing. The data provided by in-situ  
85 sensors will be of significantly higher temporal resolution, negating the need for repeated  
86 sampling surveys throughout the year, which represent an economic cost to the farmer.  
87 Furthermore, this may enable more accurate timing of fertiliser application, reducing the risk  
88 of yield penalties caused by N-nutrition deficiencies, and reducing the risk of N transfers to  
89 water and air as a result of excessive fertiliser N applications. It is also likely that the high  
90 resolution data generated by an in-situ sensor network will increase knowledge of the  
91 controls of soil N processes and thus enable development of models which allow for a  
92 proactive approach to fertiliser N management.

93           At the time of writing, there are no such quasi-permanent field sensors in use  
94 commercially. However, potential for the development and deployment of such sensors exists  
95 (Shaw et al., 2014). Ion-selective electrodes have many characteristics suitable for soil  
96 sensing networks. They are relatively cheap, simple to use, require no mains electrical power  
97 supply and the concentration of the target ion can be easily calculated via a pre-calibration.  
98 Nitrate ( $\text{NO}_3^-$ ) selective electrodes have previously been successfully deployed for  
99 monitoring streams and agricultural drainage ditches (Le Goff et al., 2002; Le Goff et al.,  
100 2003) as well as for on-the-go soil sampling of agricultural soils (Sinfield et al., 2010) and  
101 on-farm rapid tests for soil  $\text{NO}_3^-$  (Shaw et al., 2013). Direct soil measurement, which is  
102 essential for the success of in-situ monitoring, has been shown to be possible (Ito et al., 1996;  
103 Adamchuk et al., 2005), although improvements in accuracy and robustness of the sensing  
104 membrane are required. Increasing use of nano technologies for the construction of  
105 electrochemical sensors may result in significant advances in sensor performance (Arrigan,  
106 2004; Atmeh and Alcock-Earley, 2011).

107           Optimising the spatial configuration of a sensor network is needed to ensure that  
108 precise estimate of the mean across a field or management zone can be made whilst minimising  
109 economic costs. It is, therefore, important to make an assessment of the spatial variation of  
110 soil mineral N across a range of scales to determine an optimum configuration prior to  
111 implementation of the sensor network. This is particularly important in grazed grasslands  
112 where N returns from livestock occur unevenly (Bogaert et al., 2000). Since sensors must be  
113 organized in clusters around a hub with a logger, sensor networks can be regarded as multi-  
114 scale sampling schemes with hubs, the primary units, and sensors (secondary units) randomly  
115 placed in an area around each hub. As shown by de Gruijter et al. (2006), the optimum  
116 configuration of such a sampling scheme depends on the relative costs of additional primary  
117 and secondary units and the within- and between-primary unit variability. For example a field

**Commented [DLJ3]:** Some are used in glasshouse  
agronomy – hydroponic systems so I qualified to field

118 which has little large-scale variation may be served by a collection of sensors connected to  
119 one sensing hub, whereas a field with more variation at larger scales would require sensors to  
120 be located in multiple areas of the field. When determining an optimal configuration it is also  
121 important to consider the degree of uncertainty of the resulting estimations and the associated  
122 cost-benefit of reducing this uncertainty. Consideration also needs to be made as to whether  
123 the scale and magnitude of the observed in-field N variation is large enough to justify spatial  
124 variation in the optimum fertiliser input rate and, hence, the demarcation of within-field  
125 management zones.

126         As seen in the discussion above, the feasibility and optimal design of sensor networks  
127 depends on the variability of the target properties at different within-field scales. An effective  
128 way to collect such information is by spatially nested sampling. This was first used in soil  
129 science by Youden and Mehlich (1937) and rediscovered as a technique for investigation of  
130 multiscale soil variation by Webster and Butler (1976). In nested spatial sampling, sample  
131 sites are arranged in a nested hierarchical design which allows the partition of the variance of  
132 the measured variable into components associated with a set of pre-determined scales. At the  
133 highest level of the hierarchy sample, points are arranged in clusters associated with “main  
134 stations” which may be at randomly-located sites or on nodes of a grid or transect. Within a  
135 mainstation, sample points may be divided between two or three stations at level 2 which are  
136 separated from each other by some fixed distance. For example, the stations at level 2 may be  
137 on the vertices of an equilateral triangle with sides length  $d_2$  m, or at two locations  $d_2$  m apart.  
138 While these distances are fixed, the orientation of the level-2 stations relative to each other is  
139 randomized to ensure lack of bias. Within each level-2 station, sample points may be ordered  
140 at further nested spatial scales.

141         This approach has been used to investigate the distribution of nematodes in soil at  
142 within-field scales (Webster and Boag, 1992), to examine the variation of ammonia



143 volatilization from urea amended soil at within-field to landscape scales (Corstanje et al.,  
144 2008), to resolve the spatial variability of soil N mineralisation (Córdova et al., 2012), and to  
145 examine the interactions of soil and herbicide at within-field scale (Price et al., 2009).  
146 Recently, Lark (2011) showed how setting nested sampling in the linear mixed model  
147 framework allows the nested sampling scheme to be optimized in different circumstances.

148 The aim of this study was to investigate the spatial variation of plant-available N  
149 (amino acids, ammonium ( $\text{NH}_4^+$ ) and  $\text{NO}_3^-$ ) concentrations in soil within a grassland field  
150 over a 2 month period. A geo-spatial statistical approach was used to quantify the observed  
151 variation and the results were used to explore how an in-situ soil N sensor network may be  
152 optimally designed and deployed. The potential and challenges of integrating this approach  
153 within a PA framework are discussed.

154

## 155 **2. Materials and methods**

### 156 *2.1. Field site and soil characteristics*

157 The field used for this study is located within the Henfaes Research Station  
158 Abergwyngregyn, Wales, UK (53°14'N 4°01'W). The site has a temperate, oceanic climate,  
159 receives an average annual rainfall of 1250 mm and has a mean annual soil temperature at  
160 10 cm depth of 11 °C. The field is roughly rectangular with a perimeter of 559 m and an area  
161 of 1.91 ha. It has an average altitude of 12.1 m asl with a slope of 1.5 % in a northerly aspect.  
162 It is a semi-permanent sheep-grazed grassland, dominated by *L. perenne* L. The current ley  
163 was established by direct drill in April 2009 using a perennial and hybrid ryegrass mix. The  
164 field has been used for both all year round grazing and silage production since 2009,  
165 receiving an annual inorganic fertiliser input of between 100 – 130 kg N ha<sup>-1</sup> in addition to  
166 potassium (K), phosphate (P) and sulphur (S) at recommended rates. Lime has also been  
167 applied when necessary to restore the pH to a target value of 6.5. In 2014, inorganic fertiliser

168 was applied on 12/5/14 and 11/7/14 at a rate of N:P:K 50:10:10 and 60:4:0 kg ha<sup>-1</sup>,  
169 respectively. The field was grazed until 9/6/14 and the field remained sheep free until the  
170 2/9/14. The soil is a free draining Eutric Cambisol with a sandy clay loam texture and a fine  
171 crumb structure.

172 To assess the chemical characteristics of the soil, replicate samples ( $n = 4$ ) were  
173 collected from 4 blocks (30 × 30 cm) at a depth of 0 – 10 cm, representing the Ahp horizon.  
174 The soil was placed in gas-permeable polyethylene bags and transported to the laboratory in a  
175 refrigerated box. All of the following procedures were performed on the same day as field  
176 sampling. Soil pH and electrical conductivity were determined in a 1:2.5 (w/v) soil:distilled  
177 water suspension using standard electrodes. Moisture content was determined by drying for  
178 24 h at 105 °C. Total C and N were determined with a TruSpec CN analyser (Leco Corp., St  
179 Joseph, MI, USA). Dissolved organic carbon (DOC) and dissolved organic nitrogen (DON)  
180 were measured in soil extracts (0.5 M K<sub>2</sub>SO<sub>4</sub>, 1:5 w:v) using an Analytik Jena Multi N/C  
181 2100S (AnalytikJena, Jena, Germany). Chloroform fumigation and incubation ( $t = 7$  days) of  
182 2 g ( $n = 4$ ) of fresh soil was performed to determine microbial biomass C and N according to  
183 Voroney et al. (2008) ( $K_{EC} = 0.35$   $K_{EN} = 0.5$ ). Exchangeable cations were extracted using  
184 0.5 M acetic acid (Sparks, 1996) and the filtered extracts analyzed using flame emission  
185 spectroscopy (Sherwood 410 flame photometer; Sherwood Scientific, Cambridge, UK).  
186 Extractable phosphorus (P) was determined by extraction with 0.5 M acetic acid with  
187 subsequent colorimetric analysis using the molybdate blue method of Murphy and Riley  
188 (1962). Basal soil respiration was determined in the laboratory at 20 °C using an SR1  
189 automated multichannel soil respirometer (PP Systems Ltd., Hitchin, UK) and steady state  
190 CO<sub>2</sub> production rates recorded after 24 h. Potentially mineralisable N was determined using  
191 an anaerobic incubation method based on Keeney (1982). Briefly, 5 g field moist soil was  
192 place in a 50 ml centrifuge tube, which was then filled to the top with de-ionized H<sub>2</sub>O and the

193 tubes sealed. Soils were subsequently incubated in the dark at 40 °C for 7 d. The difference in  
194  $\text{NH}_4^+$  content between  $t = 0$  and  $t = 7$  d was attributed to N mineralization. Above ground  
195 biomass was sampled on 26/6/2014. Replicate  $1 \times 1$  m blocks ( $n = 4$ ) were chosen at random  
196 from within the field. The vegetation was cut to ground level, stored in paper bags and  
197 subsequently oven-dried at 80 °C to determine dry matter content. A summary of the results  
198 are shown below in Table 1.

199

## 200 2.2. Sampling design and protocol

201 *Nested sampling for spatial variability:* The sampling was designed in the light of the  
202 following considerations. The aim was to characterize the variability of forms of soil N at a  
203 range of spatial scales relevant to planning the design of an in-situ sensor network. In  
204 particular, it was necessary to examine the relative importance of variance between and  
205 within local regions each of which might be represented by a cluster of  $\text{NO}_3^-$  electrodes or  
206 similar sensors deployed around a single data logger such that the maximum distance  
207 between any two sensors is about 2 m. In a grassland environment it was expected that one  
208 source of variation would be urine patches of linear dimensions about 40 cm (Selbie et al.,  
209 2015). Otherwise we had no prior information on the likely distribution of variance between  
210 the scales of interest.

211 Given these considerations we planned a nested sampling design with length scales  
212 within each main station of 1 cm, 10 cm (intermediate between the fine scale and urine patch  
213 scale), 50 cm (urine patch scale) and 2 m (upper bound on the "within-region served by a  
214 sensor cluster" scale). We distributed mainstations by stratified random sampling with the  
215 target field divided into four quarters (strata) of equal area. Four mainstations were  
216 established at independently and randomly-selected locations within each quarter (stratum),  
217 giving a total of 16 mainstations. The design of the sampling scheme within each mainstation

218 was obtained by the optimization procedure of Lark (2011) on the assumption of a fractal or  
219 quasi-fractal process in which the variance is proportional to the log of the spatial scale. The  
220 objective function was the mean estimation variance of the variance components. Figure 1  
221 shows the optimized sample design. With 12 samples per mainstation the total sample size  
222 was 192. The sample sites were then selected at each mainstation by randomizing the  
223 direction of the vectors between the substations at each level of the design shown in Figure 1,  
224 while keeping the lengths of the vectors fixed. An initial nested sampling campaign was  
225 performed over 2 days on the 4<sup>th</sup> and 5<sup>th</sup> June, 2014. This was repeated on the 31<sup>st</sup> July and 1<sup>st</sup>  
226 August, 2014, 3 weeks after the field received a N fertiliser input of 60 kg N ha<sup>-1</sup>. Sample site  
227 locations were set up the day before sampling took place. At each sampling location a soil  
228 corer, of diameter 1 cm, was used to sample soil. A 5 cm soil core from between depths of 5 -  
229 10 cm was sampled and placed in gas-permeable plastic bags, and stored in a refrigerated  
230 box. This depth was chosen as it represents the middle of the rooting zone and would make  
231 installation of any in-situ sensor a straight forward process. Following the sampling event the  
232 samples were transferred immediately to the laboratory where they were refrigerated at 4 °C.  
233 Extraction of soluble N from soil was performed on the soil cores on the same day as  
234 sampling as described below. During the second nested sampling event, duplicate sub-  
235 sampling and chemical analysis were performed on 4 out of the 12 samples from each  
236 mainstation in order to make an assessment of measurement error.

237 To investigate spatial variability of N forms at the sub-core scale a further sampling  
238 design and protocol was developed and performed on the 25<sup>th</sup> June, 2014. Two sampling  
239 locations were chosen at random within each of the 4 strata. At each location, a pair of  
240 samples were taken, using the protocol described above, with a distance of 1 cm between  
241 each sample. This resulted in a total of 16 core samples. On return to the laboratory the cores  
242 were broken apart and 4 “aggregates” of weight 60 – 80 mg were collected (diameters ca. 1-

243 2 mm). These aggregates were then soluble N extracted and analysed using the protocol  
244 described below.

245 *Investigating depth effects:* To investigate the variability of forms of N with depth an  
246 equilateral triangle, with sides 50 cm, was randomly located within each strata. The 50 cm  
247 scale was chosen as the initial nested sampling showed that it encompassed most of the  
248 variance for all N forms. At the vertices of the triangle, a core was taken to 25 cm depth and  
249 was subsequently split into 5 cm sections, giving a total of 60 samples. This sampling was  
250 performed on the 27<sup>th</sup> June, 2014.

251

### 252 2.3. Extraction and chemical analysis of soil samples

253 All soil extractions were performed on the same day as sample collection, according  
254 to the following protocol. Samples were crumbled by hand, in order to prevent sieving  
255 induced N mineralisation (Jones and Willett, 2006; Inselsbacher, 2014). Large stones, roots  
256 and vegetation were removed prior to gentle mixing of the sample. To further reduce  
257 mineralisation of organic N forms, sub-samples of field-moist soil (2 g) were extracted on ice  
258 (175 rev min<sup>-1</sup>, 15 min) using cooled (5 °C) 0.5 M K<sub>2</sub>SO<sub>4</sub> at a soil: extractant ratio of 1:5  
259 (w:v) (Rousk and Jones, 2010). The extracts were centrifuged (4,000 g, 15 min), and the  
260 resulting supernatant collected and frozen (-18°C) to await chemical analysis. The protocol  
261 differed slightly for the soil aggregate samples. Each aggregate, of weight 60 – 80 mg, was  
262 placed in a 1.5 ml Eppendorf® micro-centrifuge tube and crumbled gently using a metal  
263 spatula. The soil was then extracted in 500 µl of 0.5 M K<sub>2</sub>SO<sub>4</sub> as described above. Total free  
264 amino acid-N was determined by the *o*-phthaldialdehyde spectrofluorometric method of  
265 Jones et al. (2002). NH<sub>4</sub>-N was determined by the salicylate-nitroprusside colorimetric  
266 method of Mulvaney (1996) and NO<sub>3</sub>-N by the colorimetric Griess reaction of Miranda et al.  
267 (2001) using vanadate as the catalyst.

268

#### 269 2.4. Statistical analysis

270 *Nested Sampling:* The  $n$  data from the nested sampling may be analysed according to  
 271 the following statistical model. An  $n \times 1$  vector of observations,  $\mathbf{y}$ , is regarded as a  
 272 realization of a random variate,  $\mathbf{Y}$ , where

$$273 \quad \mathbf{Y} = \mathbf{X}\beta + \mathbf{U}_s\eta_s + \mathbf{U}_m\eta_m + \mathbf{U}_2\eta_2 + \mathbf{U}_{0.5}\eta_{0.5} + \mathbf{U}_{0.1}\eta_{0.1} + \mathbf{U}_{0.01}\eta_{0.01} + \mathbf{U}_r\eta_r. \quad (1)$$

274  $\mathbf{X}$  is a  $n \times p$  design matrix which represents fixed effects in the model (e.g.  $p$  levels  
 275 of a categorical factor, or  $p$  continuous covariates) and  $\beta$  is a length- $p$  vector of  
 276 fixed effects coefficients. There are 4 strata in the sampling design, and  $\mathbf{U}_s$  is a  $n \times$   
 277 4 design matrix for the strata. If the  $i$ th observation is in stratum  $j$  then  $\mathbf{U}_s[i, j] =$   
 278 1 and all other elements in the  $i$ th row are zero. The design matrix associates each  
 279 observation with one of 4 random values in the random variate  $\eta_s$ . These values  
 280 are assumed to be independent and identically distributed Gaussian random variables with  
 281 a mean of zero and a variance  $\sigma_s^2$  which is the between-stratum variance component.  
 282 Similarly  $\mathbf{U}_m$  is a  $n \times 16$  design matrix for the mainstations, and the variance of  
 283  $\eta_m$  is the between-mainstation variance component. The terms with subscripts 2, 0.5, 0.1 and  
 284 0.01 represent the design matrices and random effects for the components of variation  
 285 associated with the 2-m, 0.5-m, 0.1-m and 0.01-m scales respectively. If duplicate material  
 286 from some or all of the soil specimens is analysed then the random effect  $\eta_r$  which represents  
 287 the variation due to subsampling and analytical variation can be estimated, otherwise it is a  
 288 component of the variation estimated for the finest spatial scale.

289 Under the linear mixed model  $\mathbf{Y}$  has covariance matrix  $\mathbf{H}$  where

$$290 \quad \mathbf{H} = \sigma_s^2 \mathbf{U}_s^T \mathbf{U}_s + \sigma_m^2 \mathbf{U}_m^T \mathbf{U}_m + \sigma_2^2 \mathbf{U}_2^T \mathbf{U}_2 + \sigma_{0.5}^2 \mathbf{U}_{0.5}^T \mathbf{U}_{0.5} + \sigma_{0.1}^2 \mathbf{U}_{0.1}^T \mathbf{U}_{0.1} \\ 291 \quad + \sigma_{0.01}^2 \mathbf{U}_{0.01}^T \mathbf{U}_{0.01} + \sigma_r^2 \mathbf{U}_r^T \mathbf{U}_r, \quad (2)$$

and the superscript T denotes the transpose of a matrix. The parameters of this matrix are therefore the variance components, and these can be estimated by residual maximum likelihood (REML), see Webster and Lark (2013). Once this has been done then the fixed effects coefficients in the model can be estimated by generalized least squares (see Lark and Cullis, 2004). Note that there is an explicit assumption that the data are a realization of a Gaussian random variable. For this reason the values were transformed if exploratory analysis suggested that this is not a plausible assumption.

Because all sampling could not be done in one day the sampling day was randomized within strata, so as not to be confounded with the spatial variance components of interest. For this reason it is regarded as a fixed effect in the model. The significance of the between-day effect was tested with the Wald statistic as discussed in Lark and Cullis (2004).

The significance of a random effect in the model can be tested by comparing the residual log-likelihood for a model with the term dropped ( $L^-$ ) with the residual log-likelihood for the full model (all random effects,  $L$ ). Any variance accounted for by a term which is dropped will contribute to variance at lower levels in the hierarchy (finer spatial scales) for the dropped model. For this reason the ultimate component of the model ( $\eta_r$  when there are duplicate analyses and  $\eta_{0.01}$  otherwise) cannot be dropped. Dropping a term from the model will usually reduce the log-likelihood (and will not increase it). Whether the reduction in likelihood is strong enough evidence that the inclusion of the term in the full model is justified can be assessed by computing Akaike's information criterion *AIC* for each model:

$$AIC = -2L + 2P \quad (3)$$

where  $P$  is the number of parameters in the model. The *AIC* penalizes model complexity, by selecting the model with smaller *AIC*, one minimises the expected information loss through the selection decision (Verbeke and Molenberghs, 2000).

*Aggregate scale sampling:* After any necessary transformations the  $n$  data collected to investigate variation within cores were analysed according to the following statistical model.

An  $n \times 1$  vector of observations,  $y$ , is regarded as a realization of a random variate,  $Y$ , where

$$Y = X\beta + U_s\eta_s + U_p\eta_p + U_c\eta_c + U_a\eta_a, \quad (4)$$

As in Equation (1),  $X$  is a design matrix for fixed effects and  $\beta$  is a vector of fixed effects coefficients (here just a constant mean). Again, as in Equation (1),  $U_s$  is a  $n \times 4$  design matrix for the strata and  $\eta_s$  is assumed to be an independent and identically distributed Gaussian random variate with a mean of zero and a variance  $\sigma_s^2$ . In the same way  $U_p$  and  $\eta_p$  are the design matrix and the random variate for the between-pair within stratum effect, with variance  $\sigma_p^2$ ;  $U_c$  and  $\eta_c$  are the design matrix and the random variate for the between-core within-pair component, with variance  $\sigma_c^2$  and  $U_a$  and  $\eta_a$  are the design matrix and the random variate for the between-aggregate within-core component, with variance  $\sigma_a^2$ . This latter component is effectively the residual as there are no duplicate measurements on any aggregate. The same method based on the AIC was used to assess the evidence for including each term in the model above the between-aggregate effect.

*Depth sampling:* After any necessary transformation the data were analysed by a nested linear mixed model of the form

$$Y = X\beta + U_s\eta_s + U_c\eta_c + \varepsilon. \quad (5)$$

As in previous models  $X$  is a design matrix for fixed effects, here associating each observation with one of the five depth increments. The fixed effects coefficients in  $\beta$  are therefore mean values of the target variable for each increment. As before  $U_s$  and  $U_c$  are design matrices for between-stratum and between-core-within-stratum random effects. The term  $\varepsilon$  is an identically and independently distributed random variable of mean zero, the residual. This model was fitted by REML, and Wald tests were used to test the null hypothesis of equal mean values for the depth increments.



342

## 343 2.5. Design of sensor arrays

344 The variance components derived from the nested sampling were used to examine the  
345 theoretical performance of different configurations of an in-situ sensor array, where a cluster  
346 of  $n_e$  sensors are randomly located within a region of 2 m diameter around each of  $n_l$  data  
347 logging hubs, which are located by simple random sampling. The between-sensor within-  
348 logger component of variance can be approximated by

$$349 \sigma_{\text{sens}}^2 = \sigma_2^2 + \sigma_{0.5}^2 + \sigma_{0.1}^2 + \sigma_{0.01}^2, \quad (6)$$

350 and the between-logger variance by

$$351 \sigma_{\text{log}}^2 = \sigma_s^2 + \sigma_m^2. \quad (7)$$

352 As such, the standard error of the mean can be estimated as follows:

$$353 \sigma_{\text{mean}} = \{ (\sigma_{\text{log}}^2 / n_l) + (\sigma_{\text{sens}}^2 / n n_e) \}^{1/2}. \quad (8)$$

354 The 95% confidence interval of the mean could therefore be calculated given variance  
355 components and particular values of  $n_l$  and  $n_e$  and the limits were back-transformed to the  
356 original units of measurement.

357

## 358 3. Results

### 359 3.1. Nested sampling to evaluate the spatial distribution of soluble N in soil prior to 360 application of N fertiliser

361 Table 2 shows summary statistics for amino acid,  $\text{NH}_4^+$  and  $\text{NO}_3^-$  concentrations in  
362 soil for the nested sampling undertaken over 2 days in June. Note that in all cases a Box-Cox  
363 transformation was chosen, conditional on sampling day as a fixed effect. Variance  
364 components for the different spatial scales are shown in Table 3 and the accumulated  
365 variance components, from the smallest to largest scale, are plotted in Figure 2. In total, 192  
366 samples were collected and processed over 2 days.

The results show that there was a significant difference (as assessed by the Wald statistic) between the 2 sampling days for  $\text{NH}_4\text{-N}$  concentration only. The different forms of N showed slightly different scale-dependencies, although in general, short-range variance dominated. For amino acid-N, the 1-cm scale had the largest variance component, constituting 58.6% of the total accumulated variance. The 10-cm and the between-mainstations within strata term were important spatial components as they were judged by the AIC to improve the likelihood of the model sufficiently to justify their inclusion. Similarly, for  $\text{NH}_4\text{-N}$  the 1-cm scale had the largest variance component, constituting 63.0% of the total accumulated variance. However, for spatial scales greater than 1 cm, only the between-mainstations within strata term was important as judged by the AIC. For  $\text{NO}_3\text{-N}$ , there was more variance at larger scales compared to the other forms of N, with the 10-cm scale having the largest variance component, constituting 28.0% of the total accumulated variance. Furthermore, all the spatial scales, with the exception of the 2-m scale, exhibit variance that was considered important by the AIC. Short-range scale variation still dominated though, with 70.4% of the variance occurring at spatial scales up to 50 cm. It should be noted that the 1-cm scale component will also include any measurement error.

### *3.2. Nested sampling to evaluate the spatial distribution of soluble N in soil after application of N fertiliser*

To assess the influence of nutrient management regime, a second nested sampling was undertaken in July, 3 weeks after the field had been fertilised with  $60 \text{ kg N ha}^{-1}$ . Summary statistics for soluble N in soil are shown in Table 4 and variance components for the different spatial scales are shown in Table 5.

The accumulated variance components, from the smallest to largest scale, are plotted in Figure 3. The same protocol was used as for the first nested sampling with the addition of

duplicate measurements on 4 samples from each mainstation. This allowed the 1-cm spatial  
 variance component to be resolved from the subsampling and measurement error, which is  
 the residual variance in this analysis. As this forms the ultimate term in the model, it allows  
 an assessment of the importance of the 1-cm spatial component by the AIC. For all of the N  
 forms, the 1-cm scale was considered important by the AIC, and was larger than the residual  
 variance. However, the residual variance, which was similar for all N forms, constitutes a  
 substantial component of the accumulated variance and was, for all N forms, larger than the  
 variance at 50 cm and 2 m. The different forms of N showed slightly different scale-  
 dependencies, although in general short-range variance dominated. For amino acid-N the  
 between mainstations within strata had the largest variance component, constituting 35.8% of  
 the total accumulated variance, although 57.7% of the total accumulated variance occurred at  
 scales up to 10 cm. The 1-cm, 10-cm and the between-mainstations within-strata term were  
 important as they are judged by the AIC to improve the likelihood of the model sufficiently to  
 justify their inclusion. For  $\text{NH}_4\text{-N}$ , the 1-cm scale had the largest variance component,  
 constituting 55.1% of the total accumulated variance. Spatial scales greater than 10 cm  
 accounted for only 13.3% of the total accumulated variance. Only the 1-cm and the between-  
 mainstations within-strata terms were important as judged by the AIC. For  $\text{NO}_3\text{-N}$ , the  
 variance at larger scales was similar to that of amino acids, with the between-mainstations  
 within strata scale having the largest variance component, constituting 38.7% of the total  
 accumulated variance. As for amino acid-N, the 1-cm, 10-cm and the between-mainstations  
 within-strata term were important as they are judged by the AIC. Short-range scale variation  
 still dominated though, with 61.2% of the variance occurring at spatial scales up to 50 cm.

414

### 415 3.3. Aggregate-scale variability of soluble N in soil

416 The grassland soil is characterized by small aggregates (ca. 1-2 mm diameter) relative

417 to the size of the bulk soil cores used in the nested samplings (1 cm diameter). Table 6 shows  
418 the summary statistics for the within-core, aggregate scale variability while the variance  
419 components are shown in Table 7.

420 In all cases, the largest variance component was the between-aggregate within-core  
421 scale. For  $\text{NH}_4\text{-N}$  and  $\text{NO}_3\text{-N}$ , 91.3% and 80.1% respectively of the total accumulated  
422 variance occurred at this scale, which was an order of magnitude higher than the variance at  
423 the between core scale. The variance at the aggregate scale for amino acid-N was slightly  
424 lower at 69.2%. It should be noted that any analytical error that occurred will also appear in  
425 this variance component. The between-core component, which represents the 1-cm spatial  
426 scale, was important for amino acid-N and  $\text{NO}_3\text{-N}$ , but not  $\text{NH}_4\text{-N}$ , as judged by the AIC.  
427 Neither the between-pair component, which is similar to the between-mainstations scale, nor  
428 the between-strata component were found to be important as judged by the AIC. Due to the  
429 limited replication (2 pairs of cores per strata), the results at stratum and mainstation scale  
430 should be interpreted in light of the above nested sampling results. The main interest is in the  
431 relative magnitude of the between-core within-pair and between-aggregate within-core  
432 components of variance.

433

#### 434 *3.4. Influence of depth of the variability of soluble N in soil*

435 Table 8 shows summary statistics for residuals of the Box-Cox transformed data  
436 collected from different soil depths. All forms of N showed a decreasing trend down the soil  
437 profile (Figure 4). Table 9 presents the estimated mean values for all N forms (Box-Cox  
438 transformed) for each depth increment. There is a clear reduction in the concentration of each  
439 N form with depth. The variation with depth was significant for  $\text{NH}_4\text{-N}$  and  $\text{NO}_3\text{-N}$  ( $p <$   
440 0.001) but not for amino acid-N ( $p = 0.55$ ).

441

442 3.5. *Optimisation of a within-field sensor network for monitoring soluble N in soil*

443 Figure 5 shows plots of the width of the 95% confidence interval for NO<sub>3</sub>-N using  
444 variance components from the two sets of spatially nested samples. These were computed for  
445  $n_l=1-10$  loggers with  $n_e=2-15$  sensors distributed equally among the loggers, 15 being the  
446 maximum number of sensor ports on the data logger (DL2e DeltaT, Cambridge, UK). The  
447 total cost for each configuration is shown on the abscissa of the plot, on the basis of unit costs  
448 of £2000 and £200 respectively for a data logger (DL2e DeltaT, Cambridge, UK) and an  
449 ELIT NO<sub>3</sub><sup>-</sup> electrode with a coupled reference electrode (ELIT 8021, ELIT 003, Nico2000,  
450 Harrow, UK). The form of these curves reflects the distribution of the variance of NO<sub>3</sub>-N  
451 over the spatial scales. Note that the width of the confidence interval is largest for the June  
452 observations, so discussion is focussed on these. Note also, as described in the Figure caption,  
453 that some points are excluded from the plot (small numbers of sensors on small numbers of  
454 loggers) to allow both graphs to be displayed with the same range of values on the ordinate.

455 The graphs show how both increasing the number of sensors per logger, and  
456 increasing the number of loggers, reduces the width of the confidence interval. Note that  
457 reducing this width substantially below 1 µg N g<sup>-1</sup> dry soil would require substantial costs,  
458 with small marginal improvement on increasing the size of the array. To reduce the width of  
459 the confidence interval to 0.5 µg N g<sup>-1</sup> dry soil requires 10 loggers with 11 sensors each at a  
460 cost of £22,200.

461 The graphs allow different options for the design of arrays to be explored. If, for  
462 example, we required the width of the 95% confidence interval to be no wider than 1 µg N g<sup>-1</sup>  
463 dry soil then the options include the use of 3 loggers with 11 sensors per logger, 4 loggers  
464 with 5 sensors per logger or 5 loggers with 4 sensors per logger. The costs of these options  
465 are £8,200, £9,000 and £10,800 respectively. This quality measure cannot be achieved with  
466 just one or two loggers. The rational choice of array configuration is therefore 3 loggers with

11 sensors on each. Consider an alternative situation where the budget was fixed at £5,000. This could be used to provide a single logger with 15 sensors on each, or two loggers with 5 sensors on each. The width of the confidence interval for these two options is  $\pm 2.12$  and  $\pm 1.69 \mu\text{g N g}^{-1}$  dry soil respectively, so the second option is the rational choice.

The discussion above highlights that, with increasing budget, it is not necessarily rational to use the maximum number of sensors on a logger before changing to an array with an extra logger. However, once three or more loggers are in use,  $n_l \geq 3$ , an array of  $15n_l$  sensors is always more efficient than any array of equal or lesser total cost with more than  $n_l$  loggers.

## 4. Discussion

### 4.1. Spatial variation of soluble N at within-field scales

An assessment of the spatial variation of amino acid-N,  $\text{NH}_4\text{-N}$  and  $\text{NO}_3\text{-N}$  at within-field scales was determined using a nested sampling approach. Short-range variation was found to be dominant, with at least 61%, 86% and 61% of the total accumulated variance amino acid-N,  $\text{NH}_4\text{-N}$  and  $\text{NO}_3\text{-N}$ , respectively, attributed to scales  $< 2$  m. The aggregate-scale sampling revealed further large variation at the sub 1-cm scale, which was considerably higher than the variation attributed to the 1-cm scale for all N forms. Although short-range variation dominated, variation at larger scales was not negligible and the within-strata, between-mainstation scale was considered an important spatial component for all N forms.

It is likely that the observed variation at scales  $< 2$  m is primarily due to the relatively random and uneven deposition of N from sheep excreta. Similar small-scale variation of  $\text{NO}_3\text{-N}$  in grazed pastures has been identified in previous studies, with semi-variograms exhibiting the range of spatial dependency  $< 5$  m (White et al., 1987; Broeke et al., 1996; Wade et al., 1996; Bogaert et al., 2000), and a nugget variance of 60 % (Bogaert et al., 2000).

492 These results contrast with similar studies performed on arable soils, which were  
493 characterised by ranges of spatial dependencies for  $\text{NO}_3\text{-N} > 39 \text{ m}$  (Van Meirvenne et al.,  
494 2003; Haberle et al., 2004).

495         Given that the linear dimension of a urine patch is approximately 40 cm, it is unlikely  
496 that the observed variation at the 1-cm and “aggregate” scales is driven by the uneven  
497 deposition of sheep excreta. Previous studies of spatial variation in soil N, in the context of  
498 within-field scales, have not investigated variation over such small scales. Variation at these  
499 scales is unlikely to have any significance for agronomic management as most soil sampling  
500 is conducted using large soil cores (ca. 2-10 cm diameter) with subsequent bulking of  
501 samples to ensure that small scale variation is encompassed. This small-scale variation is  
502 likely due to the inherent micro-heterogeneity of soil properties, for example, the abundance  
503 of plant roots and mycorrhizal hyphae (Stoyan et al., 2000), availability of labile organic  
504 matter (Parkin, 1987; Wachinger et al., 2000), earthworm channels and the composition and  
505 abundance of the microbial community (Grundmann and Debouzie, 2000; Nunan et al.,  
506 2002), which in turn will affect biogeochemical processes controlling soil N concentrations.  
507 The proportion of the total accumulated variance attributed to the 1-cm scale was much larger  
508 for amino acid-N and  $\text{NH}_4^+\text{-N}$  than  $\text{NO}_3\text{-N}$  which may be related to their relative diffusion  
509 coefficients, interactions with the solid phase (Owen and Jones, 2001) and the rapid rate of  
510 amino acid turnover and mineralisation in this soil (Jones et al., 2004; Wilkinson et al., 2014).  
511 The observed variation at larger spatial-scales within this study, could be due to the habit of  
512 sheep to frequent certain areas of the pasture such as paths, a drinking trough and areas of  
513 shade (Bogaert et al., 2000).

514         Variation with soil depth was also apparent, with all N forms showing a consistent  
515 reduction in concentration with increasing depth, although this was not considered a  
516 significant effect for amino acids. Decreasing concentrations of inorganic N down the soil

517 profile is well characterised in the literature (Van Meirvenne et al., 2003; Wall et al., 2010)  
518 and can be attributed to inputs of N via leaf litter, rainfall, animal excreta and fertilisers to the  
519 soil surface as well as being the site where maximal root turnover exists.

520       There was also some suggestion of a spatio-temporal interaction as evidenced by  
521 small differences in the spatial dependencies of the N forms between the June and July nested  
522 sampling events. In the case of NO<sub>3</sub>-N, the total accumulated variance was lower, with more  
523 of the observed variance attributed to scales > 2 m for the July sampling. This change may be  
524 attributed to the removal of sheep and the associated local inputs of N, combined with N  
525 fertilisation of the field (60 kg N ha<sup>-1</sup>) that occurred 3 weeks prior to the second nested  
526 sampling event.

527

#### 528 *4.2. Optimisation of planning a within-field soil N sensor network*

529       This study clearly demonstrates how nested sampling combined with geostatistical  
530 analysis can be used to explore how varying sensor-logger numbers and configurations affect  
531 the degree of accuracy of a field mean estimation. Furthermore, given knowledge of logger  
532 and sensor costs it is possible to rationalise planning decisions on a cost-accuracy basis.  
533 Given the unit costs of £2000 and £200 respectively for a data logger and NO<sub>3</sub><sup>-</sup> ISE, the field  
534 mean for NO<sub>3</sub>-N concentration could be estimated with a 95% confidence interval no wider  
535 than  $\pm 1 \mu\text{g N g}^{-1}$  for a cost of £8,200. This would represent a significant cost to the farmer  
536 and may prevent anything significant uptake of the technology. The data logger and NO<sub>3</sub><sup>-</sup>  
537 ISEs used for the cost calculation were chosen as they were used previously in this thesis  
538 (*Articles III & IV*). There is currently a wide range of similar devices, with a range of costs,  
539 currently on the market so the figures for the cost of implementing a sensor network  
540 described above should not be considered absolute. Furthermore, it is likely that the cost of  
541 the technology will continue to fall.



It is important to note that the data used for these calculations was derived from the nested sampling which used a soil corer of 1 cm diameter. As such, these calculations are based on the assumption that any given sensor used for the within-field network would have a similar sized sampling volume. Results derived from the aggregate-scale sampling exhibited variation at the sub 1-cm scale, which for  $\text{NH}_4\text{-N}$  and  $\text{NO}_3\text{-N}$  was an order of magnitude larger than the 1-cm scale. This will have significant implications when using sensors with sensing areas of size  $< 1$  cm. More local replication at the sub 1-cm scale and hence an increase in the size of sensor arrays would be required for an acceptable level of accuracy to be achieved, resulting in increased costs. To explore optimisation of a network of sensors with sensing areas  $< 1$  cm, further sampling using sample volumes of  $< 1$  cm would be required. Ideally this would involve a similar level of replication, across all scales, to that which was used in the July nested sampling campaign. This evidence may also be quite instructive for optimising sensor design, as sensors with larger sampling areas will encompass more of this small-scale variation.

Within this optimisation, no consideration has been made to the observed depth effects. The resulting field mean is therefore, only applicable to the 5-10 cm depth. Rooting depth, and therefore, nutrient uptake, in fields adjacent to the study site has previously been observed to a depth of 30 cm (Jones et al., 2004). As such, any quantification of plant-available N derived from the sensor network should be adjusted for observed depth effects. In the case of cereals, which may root to depths  $>1.5$  m, both topsoil and subsoil sensors will probably be required to avoid bias and gain a representative pattern of soluble N within the field. Logistically, however, the deployment of sensors in subsoils represents a significant challenge.

#### *4.3. Potential for precision agriculture*

567           Integration of this approach it to a PA framework requires some further consideration.  
568 PA, with regard to N management, has often focused on within-field spatial variation and the  
569 identification of management zones to enable variable rate fertilisation, which is often  
570 referred to as site-specific N management (SSNM) (Ferguson et al., 2002; Franzen et al.,  
571 2002; Bongiovanni and Lowenberg-DeBoer, 2004; Cui et al., 2008). As the field used in this  
572 study was broadly homogenous in its soil type and topography, which was reflected in the  
573 observed small variation of soil N at large scales, it was considered more suitable to treat the  
574 field as a single management unit with a singular mean value rather than impose MZs.  
575 However, the importance of temporal variation for N management should not be  
576 underestimated. Temporal variations in growing conditions, both within and between seasons  
577 may lead to considerable differences in optimum N fertiliser requirement and hence,  
578 inefficiencies in N fertiliser-use if temporal variations are not considered (Lark et al., 2003;  
579 McBratney et al., 2005; Shahandeh et al., 2005; Shanahan et al., 2008; Deen et al., 2014).

580           It is important to consider how the approach used in this study could be applied to  
581 field exhibiting significant random and non-random (i.e. a gradient) large-scale variation,  
582 which might benefit from SSNM. It is possible that management zones could be delimited  
583 based on *a priori* knowledge of variables that may affect or indicate soil N status such as  
584 topography (Kravchenko and Bullock, 2000), soil type (Moral et al., 2011), yield variability  
585 (Diker et al., 2004) and farmers knowledge (Fleming et al., 2000). Alternatively, proximal or  
586 remote sensing, such as electromagnetic induction, may allow rapid and cost effective  
587 identification of large scale heterogeneity of soil physical properties (Hedley et al., 2004;  
588 King et al., 2005). However, the extent to which these variables correlate to soil N  
589 concentration is likely to be site specific and so may require some ground truthing. The need  
590 for management zones should become apparent from exploratory sampling but accurate  
591 delimitation of areas with significantly different soil N concentration may require sampling at

592 a finer resolution by increasing the extent of the stratification accordingly. A further broad  
593 question which needs to be addressed with respect to management zones, is at what point  
594 does the magnitude and the spatial-scale of soil N variation become sufficiently large enough  
595 to justify site-specific agriculture?

596 The success of the approach used here to optimise a sensor network and that of any  
597 management zone based system requires temporal stability of spatial variation (Sylvester-  
598 Bradley et al., 1999; Shi et al., 2002). Given significant spatio-temporal interaction, the  
599 results from any sensor network could no longer be considered accurate or precise. In this  
600 study there was evidence of a slight spatio-temporal interaction which was related to the  
601 removal of sheep from the field and the application of N fertiliser. An alternative approach to  
602 that advocated here, would be the implementation of a grid network, with sensor arrays at  
603 each node to account for small-scale soil variation. This would enable temporal, large-scale  
604 spatial variation and their interaction to be monitored. Kriging techniques could then be used  
605 to produce dynamic maps of soil N concentrations which could be used to inform variable-  
606 rate fertiliser management. However, this approach is likely to require significantly more  
607 sensing units and hubs with a resulting cost increase.

608

## 609 **5. Conclusions**

610 In this study, the spatial variation of amino acids,  $\text{NH}_4^+$  and  $\text{NO}_3^-$  within the soil of a  
611 grazed grassland field was investigated using a nested sampling approach and geo-statistical  
612 analysis. Variation at small scales ( $< 2$  m) was shown to be dominant, with further large  
613 variance evident at scales  $< 1$  cm. The observed variation was attributed to the random input  
614 of N to the soil via sheep excreta and the inherent heterogeneity of soil at the aggregate scale.  
615 Optimising the deployment of in-situ soil sensors, on the basis of accuracy and cost, was  
616 demonstrated using data derived from the nested sampling and showed that achieving

617 accurate estimates of the field mean comes at a considerable cost. Whilst the cost of  
618 technology is likely to decrease, investigation of how best to integrate this approach within a  
619 PA framework to improve NUE is still required.

620

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625

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815 **Figure legends**

816 **Fig. 1.** The optimised sampling design of a mainstation. Distances between sampling points  
817 were fixed but angles were randomized, with the exception of the 2 m vectors.

818 **Fig. 2.** Accumulated variance components from the finest to coarsest spatial scale, derived  
819 from 5<sup>th</sup> and 6<sup>th</sup> June nested sampling results (before fertiliser addition). Source is the  
820 spatial-component in meters, with M and S representing the between-mainstation and  
821 between-strata components respectively.

822 **Fig.3.** Accumulated variance components from the finest to coarsest scale, derived from 31<sup>st</sup>  
823 July and 1<sup>st</sup> August nested sampling results (after fertiliser addition). Source is the  
824 spatial-component in meters, with M and S representing the between-mainstation and  
825 between-strata components respectively.

826 **Fig. 4.** Variability of amino acid-N, ammonium-N and nitrate-N with soil depth. Data points  
827 represent means  $\pm$  SEM (n = 12) of soil N concentrations for each 5 cm depth  
828 increment.

829 **Fig. 5.** Width of the 95% confidence interval for alternative sensor arrays of different cost  
830 computed from variance components from nested sampling of nitrate N in (a) June  
831 (before fertiliser addition) and (b) July-August (after fertiliser addition). Note that the  
832 arrays comprise 1–10 loggers and a maximum of 15 sensors per logger. To allow a  
833 common range of values on the ordinates of these graphs, and to facilitate  
834 interpretation, arrays with fewer than five sensors in total have been excluded from  
835 Figure 5(a) and arrays with fewer than three sensors have been excluded from Figure  
836 5(b).